

25. Converge absolutamente pelo teste da integral.

27. Diverge; $a_n \not\rightarrow 0$

29. Converge absolutamente pelo teste da razão.

31. Converge absolutamente; $\frac{1}{n^2 + 2n + 1} < \frac{1}{n^2}$ 33. Converge absolutamente, já que $\left| \frac{\cos n\pi}{n\sqrt{n}} \right| = \left| \frac{(-1)^{n+1}}{n^{3/2}} \right| = \frac{1}{n^{3/2}}$ (p -série convergente)35. Converge absolutamente pelo teste da raiz. 37. Diverge; $a_n \rightarrow \infty$ 39. Converge condicionalmente; $\sqrt{n+1} - \sqrt{n} = 1/\left(\sqrt{n} + \sqrt{n+1}\right) \rightarrow 0$, mas as séries de valores absolutos divergem (compare com $\sum(1/\sqrt{n})$)41. Diverge; $a_n \rightarrow 1/2 \neq 0$ 43. Converge absolutamente; $\operatorname{sech} n = \frac{2}{e^n + e^{-n}} = \frac{2e^n}{e^{2n} + 1} < \frac{2e^n}{e^{2n}} = \frac{2}{e^n}$, um termo de uma série convergente.45. $|\text{Erro}| < 0,2$ 47. $|\text{Erro}| < 2 \times 10^{-11}$ 49. 0,5403051. (a) $a_n \geq a_{n+1}$ (b) $-1/2$

Seção 11.7

1. (a) $1, -1 < x < 1$ (b) $-1 < x < 1$ (c) nenhum3. (a) $1/4, -1/2 < x < 0$ (b) $-1/2 < x < 0$ (c) nenhum5. (a) $10, -8 < x < 12$ (b) $-8 < x < 12$ (c) nenhum7. (a) $1, -1 < x < 1$ (b) $-1 < x < 1$ (c) nenhum9. (a) $3, -3 \leq x \leq 3$ (b) $-3 \leq x \leq 3$ (c) nenhum11. (a) ∞ , para qualquer valor de x (b) para qualquer valor de x (c) nenhum13. (a) ∞ , para qualquer valor de x (b) para qualquer valor de x (c) nenhum15. (a) $1, -1 \leq x < 1$ (b) $-1 < x < 1$ (c) $x = -1$ 17. (a) $5, -8 < x < 2$ (b) $-8 < x < 2$ (c) nenhum19. (a) $3, -3 < x < 3$ (b) $-3 < x < 3$ (c) nenhum21. (a) $1, -1 < x < 1$ (b) $-1 < x < 1$ (c) nenhum23. (a) $0, x = 0$ (b) $x = 0$ (c) nenhum25. (a) $2, -4 < x \leq 0$ (b) $-4 < x < 0$ (c) $x = 0$ 27. (a) $1, -1 \leq x \leq 1$ (b) $-1 \leq x \leq 1$ (c) nenhum29. (a) $1/4, 1 \leq x \leq 3/2$ (b) $1 \leq x \leq 3/2$ (c) nenhum31. (a) $1, (-1 - \pi) \leq x < (1 - \pi)$
(b) $(-1 - \pi) < x < (1 - \pi)$ (c) $x = -1 - \pi$ 33. $-1 < x < 3, 4/(3 + 2x - x^2)$ 35. $0 < x < 16, 2/(4 - \sqrt{x})$ 37. $-\sqrt{2} < x < \sqrt{2}, 3/(2 - x^2)$ 39. $1 < x < 5, 2/(x - 1), 1 < x < 5, -2/(x - 1)^2$ 41. (a) $\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \frac{x^8}{8!} - \frac{x^{10}}{10!} + \dots$; converge para qualquer valor de x (b) e (c) $2x - \frac{2^3 x^3}{3!} + \frac{2^5 x^5}{5!} - \frac{2^7 x^7}{7!} + \frac{2^9 x^9}{9!} - \frac{2^{11} x^{11}}{11!} + \dots$ 43. (a) $\frac{x^2}{2} + \frac{x^4}{12} + \frac{x^6}{45} + \frac{17x^8}{2.520} + \frac{31x^{10}}{14.175}, -\frac{\pi}{2} < x < \frac{\pi}{2}$
(b) $1 + x^2 + \frac{2x^4}{3} + \frac{17x^6}{45} + \frac{62x^8}{315} + \dots, -\frac{\pi}{2} < x < \frac{\pi}{2}$

Seção 11.8

1. $P_0(x) = 0, P_1(x) = x - 1, P_2(x) = (x - 1) - \frac{1}{2}(x - 1)^2$
 $P_3(x) = (x - 1) - \frac{1}{2}(x - 1)^2 + \frac{1}{3}(x - 1)^3$ 3. $P_0(x) = \frac{1}{2}, P_1(x) = \frac{1}{2} - \frac{1}{4}(x - 2)$
 $P_2(x) = \frac{1}{2} - \frac{1}{4}(x - 2) + \frac{1}{8}(x - 2)^2$
 $P_3(x) = \frac{1}{2} - \frac{1}{4}(x - 2) + \frac{1}{8}(x - 2)^2 - \frac{1}{16}(x - 2)^3$ 5. $P_0(x) = \frac{\sqrt{2}}{2}, P_1(x) = \frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2} \left(x - \frac{\pi}{4} \right)$
 $P_2(x) = \frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2} \left(x - \frac{\pi}{4} \right) - \frac{\sqrt{2}}{4} \left(x - \frac{\pi}{4} \right)^2$
 $P_3(x) = \frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2} \left(x - \frac{\pi}{4} \right) - \frac{\sqrt{2}}{4} \left(x - \frac{\pi}{4} \right)^2 - \frac{\sqrt{2}}{12} \left(x - \frac{\pi}{4} \right)^3$ 7. $P_0(x) = 2, P_1(x) = 2 + \frac{1}{4}(x - 4)$
 $P_2(x) = 2 + \frac{1}{4}(x - 4) - \frac{1}{64}(x - 4)^2$
 $P_3(x) = 2 + \frac{1}{4}(x - 4) - \frac{1}{64}(x - 4)^2 + \frac{1}{512}(x - 4)^3$
9. $\sum_{n=0}^{\infty} \frac{(-x)^n}{n!} = 1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} + \frac{x^4}{4!} - \dots$
11. $\sum_{n=0}^{\infty} (-1)^n x^n = 1 - x + x^2 - x^3 + \dots$
13. $\sum_{n=0}^{\infty} \frac{(-1)^n 3^{2n+1} x^{2n+1}}{(2n+1)!}$ 15. $7 \sum_{n=0}^{\infty} \frac{(-1)^n x^{2n}}{(2n)!}$ 17. $\sum_{n=0}^{\infty} \frac{x^{2n}}{(2n)!}$
19. $x^4 - 2x^3 - 5x + 4$ 21. $8 + 10(x - 2) + 6(x - 2)^2 + (x - 2)^3$
23. $21 - 36(x + 2) + 25(x + 2)^2 - 8(x + 2)^3 + (x + 2)^4$ 25. $\sum_{n=0}^{\infty} (-1)^n (n+1)(x-1)^n$ 27. $\sum_{n=0}^{\infty} \frac{e^2}{n!} (x-2)^n$ 33. $L(x) = 0, Q(x) = -x^2/2$ 35. $L(x) = 1, Q(x) = 1 + x^2/2$ 37. $L(x) = x, Q(x) = x$