

# COMPLETED GROUP ALGEBRAS OF FREE-BY- $\mathbb{Z}_p$ PRO- $p$ GROUPS

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## Abstract:

The class of finitely generated free-by- $\mathbb{Z}_p$  pro- $p$  groups comprise an important family of pro- $p$  groups of cohomological dimension at most 2, amongst which one can find free pro- $p$  and Dëmushkin groups. In this talk I will present (in joint work with A. Jaikin) how those groups are virtually mild in the sense of Labute and how they are characterized by possessing a very particular type of presentation. Moreover, I will also explain how a strong control of the restricted Lie algebra structure obtained by these presentations allows us to virtually construct an explicit embedding of the completed  $F_p$ -group algebra into a division ring. As a corollary, one obtains a virtual solution to the Atiyah conjecture for this class of groups.