

# $\sigma$ -Anti-automorphisms on Graded Primitive Associative Algebras

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## Abstract

Let  $G$  be a group and  $\mathbb{F}$  a field. In [1], Bahturin, Bresar and Kochetov characterized primitive  $G$ -graded associative rings ( $\mathbb{F}$ -algebras) with a minimal  $G$ -graded left ideal and used this characterization to study graded anti-automorphisms. Afterwards, in [3], to  $G$  an abelian group and  $\sigma : G \times G \rightarrow \mathbb{F}^\times$  an anti-symmetric 2-cocycle, K. Sousa and I. Sviridova presented a similar characterization to primitive  $G$ -graded associative rings ( $\mathbb{F}$ -algebras) with a minimal  $G$ -graded right ideal in terms of  $\sigma$ -adjoints related to nondegenerate graded bilinear forms.

In this talk we use the characterization of Sousa and Sviridova and present a description of  $\sigma$ -anti-automorfismos on  $G$ -graded associative  $\mathcal{S}$ -algebras with a minimal  $G$ -graded right ideal when  $\mathcal{S}$  is an unitary commutative associative ring with trivial  $G$ -grading,  $\mathbb{U}(\mathcal{S})$  is the set of all invertible elements of  $\mathcal{S}$  and  $\sigma : G \times G \rightarrow \mathbb{U}(\mathcal{S})$  is an anti-symmetric 2-cocycle. This work is joint with I. Sviridova.

## References

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